## Guess the Ages

PROBLEM: At a party the guest asks his host the ages of his three daughters. The host replies that the product of their ages is 72 and the sum of their ages is the same as the house number. The guest checks the house number and returns to the host. "You have not given me enough information." The host replies, "The oldest daughter likes strawberry pudding." With that the guest announces the ages of the daughters. What are the ages and how did the guest figure them out?

## SOLUTION:

| Numbers | Sum |
| :--- | ---: |
| $1 \times 1 \times 72$ | 74 |
| $1 \times 2 \times 36$ | 39 |
| $1 \times 3 \times 24$ | 28 |
| $1 \times 4 \times 18$ | 23 |
| $1 \times 6 \times 12$ | 19 |
| $1 \times 8 \times 9$ | 18 |
| $2 \times 2 \times 18$ | 22 |
| $3 \times 2 \times 12$ | 17 |
| $4 \times 2 \times 9$ | 15 |
| $8 \times 3 \times 3$ | 14 |
| $6 \times 4 \times 3$ | 13 |
| $6 \times 6 \times 2$ | 14 |

ANSWER: 8,3,3
Since the guest knew the house number, he was able to eliminate all of the possibilities in which the sum wasn't equal to that number. However, even after seeing the house number, he said that he needed more information. So, it is obvious that there must be at least two possible solutions with the same sum. The only sum shared was 14 , so the answer must either be $8 \times 3 \times 3$ or $6 \times 6 \times 2$. When the host said something about his oldest daughter, $6 \times 6 x 2$ is eliminated because that would mean there would be two oldest daughters.

